STRESS-STRAIN ANALYSIS IN THE SOIL SAMPLE DURING LABORATORY TESTING

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Abstract. During the determination of soil strength and compressibility in a laboratory by different apparatus soil is loaded in a different way. It has an influence on stress-strain distribution in a sample. Some factors are not evaluated during the results interpretation, for example, friction between soil and device metal parts. The finite-element method analysis also shows that during triaxial, oedometer, shear box tests distribution of stress and strain in the sample is non-uniform. A special apparatus was designed and used for determining horizontal component of stress in the cross-section of the sample. It was determined for sands that horizontal component of stress in the cross-section centre is significantly smaller than at the edges. Increasing load plastic deformations are developing not in the whole sample but in particular places. If we know a real distribution of stress and strain in the sample, it is possible to determine the soil strength and deformation parameters in a more precise way or to rate the influence of different factors on soil properties.

Keywords: stress-strain distribution, triaxial test, oedometer, shear box, finite-element method, soil strength.

1. Introduction

Mechanical properties of soils were determined by different types of apparatus. Different stress-strain distribution was obtained using various apparatus. Boundary conditions are not distinct when analysing soil samples by oedometer and shear box. It is not obvious a stress distribution within oedometer soil specimen when applying vertical load, a part of vertical load descends to shear ring pane. Not all vertical load applied to top of shear box specimen is transmitted to soil. It is not evident the regularity of change of normal stresses on a shear plane. If an oedometer test is analysed, stress distribution in soil sample depends on the following: manner of load transmission, manner of ring embedding in apparatus (with fixed or floating ring). If a shear box test is analysed, the stress distribution depends on the following: manner of vertical load transmission, position of the mobile part of shear ring, horizontal displacement of the mobile part of the ring.

It is more precise to model stress and strain state in the soil using a triaxial apparatus. Triaxial test is the most widely used test method for determining the strength and stress-strain properties of soil. It is assumed that soil specimen deforms uniformly during the test. The uniformity of stress and strain in the specimen is the main idea of triaxial test. However, it is not often the case that a specimen in triaxial apparatus deforms uniformly during the test. Non-uniformity can be caused by the end restraint, insufficient drainage, membrane effects, soil compression, preparation of soil specimen, self-weight [1–5]. What is stress and strain distribution in soil sample, when a load is transmitted in a provided way? What influence does a non-uniformity have on the strength and stress-strain parameters of soil?

2. Review of references of laboratory testing

K. H. Head suggests that due to friction near the platen a so-called „dead zone” is formed between triaxial sample ends and the platen [6]. That „dead zone” causes a non-uniform distribution of stress and strain and non-uniform distribution of pore pressure in case of an undrained test. The use of lubricated ends eliminates „the dead zones” and protects from a wrong increase in measured strength due to the end restraint. The length of sample should be decreased from the standard ratio of height and diameter 2:1 to 1:1. This decrease is necessary to ensure an effective lubrication. It influences a more uniform stress and strain distribution [6–8], the sample may retain its cylindrical shape even at large strains. Measured strains and volume changes at failure are larger and probably demonstrate the behaviour of soil mass than those from conventional tests. Another advantage of eliminating friction is that it decreases lateral forces on triaxial cell piston [6].

Triaxial sample end restraint protects the sample from moving sideways freely and causes shear stress at the ends of the sample. Thus, the stress and strain states are not uniform within the sample. Therefore there are difficulties in interpreting test results. Experiments findings showed an influence of end restraint on shear strength of soils. The difference between the shear strength of soil sample, when the friction is eliminated by
lubricating platen ends, is not considerable if the height and diameter ratio (H/D) of the sample is larger than 2. Norris, Lee, Lade, Rowe ir Barzen found that in the samples with a H/D ratio of 2 to 1 without friction the volume change at failure is higher by about 1–1.5 % than in those without lubricated ends [6]. Bishop ir Green voted that the dilations of soils are practically the same both in lubricated ends and in those with the friction [9]. These discrepancies may be caused by the difference of axial strains at failure. Discrepancies of this kind were also found in previous studies. Raju and his colleagues presented more reliable explanations for the non-uniform results [10]. For the samples without end lubrication, axial strains and volume change occur in the middle of the sample, while their calculations are made according to the values of the whole sample, even though the latter being lower than those in the middle part.

Lubrication method using silicone between two rubber membranes is sufficiently reliable to eliminate end restraints in triaxial tests [11, 12]. Scientists have carried out triaxial tests using Fulung, Ottawa and Tamsui River types of sands. Higher peak strengths were generally found in the samples without lubrication. The volume change of the triaxial sample at failure of the sands, either dilation or compression, were higher in the samples with lubricated ends. The volume changes of the samples with and without end lubrication were rather uniform within the sample before the peak strength was reached. When the peak strength was reached and past, the volume change of the samples without end lubrication at the middle part of the sample was considerably higher. The particle breakage within the samples with lubricated end platens was quite uniform throughout the test. However, the particle breakage within the samples without end lubrication was significantly larger at the middle portion of the sample and after the peak [13].

D. W. Airey suggests that the non-uniformity occurs in triaxial samples during isotropic consolidation. He says that uniformity of deformation and stress can only be guaranteed if frictionless ends are used [14]. B. Jeremic, Z. Yang, S. Sture investigated the behaviour of elastic-plastic specimens during testing in a triaxial apparatus. They determined that inclination of end platens can cause significant non-uniformities in stress distribution inside specimen. The specimen is distorted sideways and the plastic zone remains significantly larger than in the level end platen case. Development of plastic zone for a specimen with fixed level end platens begins in the centre of specimen and remains sizable to the specimen ends. For the specimens with friction ends the plastic zone begins at the ends and extends to middle of specimen [15].

H. Sun, J. F. Chen, X. R. Ge used computerised tomography or commonly known by its medical name an X-ray scanner. This method demonstrates the attenuation of an X-ray through soil specimen and density of specimen. The lower density bands appeared in the centre of specimen at a lower confining pressure and spread to the edge due to the weak internal coherence. At higher confining pressure the lower density bands started at the edge and spread to the centre of triaxial due to strong internal coherence of sample [16]. J. Otani, T. Mukunoki, M. Yoshimura also used a new triaxial compression apparatus with the X-ray scanner. After consolidating, the initial condition of the soil sample was scanned before applying the compression. According to the initial condition, the sample cannot be considered homogeneous due to insufficient saturation. The density around the centre of the sample is lower. Low density zones first form in the middle of the sample, later other low density zones start and that is strain localisation. It is simple to determine that the local shear areas start from the bottom of the sample and expand towards the sample edges. With the strains increasing, the shear areas of the sample go upwards, from the bottom of the sample towards the top [17].

C. K. Januskevicius and E. Vey for measuring stresses and strains in triaxial sample used embedded gauges. Samples were 12.7 cm in diameter and 27.94 cm in height. They were vertically loaded at constant rate of strain and confined by horizontal pressure. The results of the strain-gauge show a non-uniformity of strain along the sample length. In the middle of the sample (at its axis) the strains were found to be higher than the average ones, whereas they were less than average at the distance of 3.81 cm from the sample ends (at its axis). The strains were lower at the distance of 3.81 cm from the sample bottom than at the same distance from the sample top (at its axis). The strains were gauged at mid-height of the sample and at 3.81 cm radius positions from the sample centre. The results demonstrate that strains at the centre of the sample are only insignificantly larger than those at the edge [18].

A. Drescher and I. Wardoulakis maintain that bulging and shear band formation depend on the sample density. A dense sample is more sensitive to these forms of strain inhomogeneities [19]. Researchers presume that in medium-dense and loose sand samples shear bands do not appear and the sample may be deformed uniformly even at large strains [20].

Strength and deformation parameters depend on stress-strain distribution in the case of the symmetrical stress distribution about axis. Using stresses \( \sigma_2 = \text{max} \) and in other case \( \sigma_2 = \text{min} \), different soil mechanical properties are obtained [21].

D. Sheng and his colleagues analysed soil stress and strain inhomogeneities in a triaxial sample caused by end restraint in drained and undrained tests, also at insufficient drainage in drained test. The stresses were measured in three aspects. First, when the soil sample end, contact with platen is perfectly smooth, without friction (SC) (Fig 1 a, d, g); secondly, when there is friction (FC) between sample ends and platens (Fig 1 b, e, h); and third, when the contact is rough (RC) (Fig 1 c, f, i). For that purpose a slightly overconsolidated Swedish clay was used. The analysis was carried out using numerical method, by applying the commercial program ABAQUS [1].

The distribution of effective axial stress \( \sigma_a \) (kPa) in specimens for drained tests can be seen in Fig 1 (qualitative view). The maximum values of effective axial stresses take place at the end edges and the minimum near \( \frac{1}{2} \) height of the lateral surface of the specimen [1].
3. Theoretical analysis of stress distribution in soil specimen using a numerical method

In order to analyse stress and strain distribution in soil sample during the oedometer and shear box tests a numerical modelling was carried out by COSMOS/M programme. A finite element models are presented to simulate the testing procedures. The formulation of a linear static problem for solution by the displacement method is fully described by the matrix equation:

$$[K][U] = [F],$$

(1)


The nodal displacements are calculated according to formula:

$$[U] = [K]^{-1}[F].$$

(2)

Then the vector of elements nodal displacements $[u_K]$ is found. By using the matrix of elements geometrical properties $[B_K]$, the elements deformations are obtained:

$$[e_K] = [B_K][u_K].$$

(3)

The stresses of finite elements are obtained, when elements deformations and stiffness matrix of elements material $[K_{elem}]$, in which the information about characteristics of material elasticity $E$, $\nu$, is known:

$$[\sigma_K] = [K_{elem}][e_K].$$

(4)

The following parameters were used for the sand specimen: elasticity modulus – 20 MPa, mass density – 1.85 Mg/m³, Poisson’s ratio – 0.3. The oedometer sample, 0.0875 m in diameter and 0.035 m in height, was discretised into 4-node two dimensional elements (Fig 2) with symmetric loading. Only two translatational degrees of freedom per node were considered for structural analysis. Two principal diagrams were designed: a) oedometer with fixed ring and stiff stamp, displacement $u_y = const$ uniformly vertically acts on the top surface of the oedometer; b) oedometer with fixed ring and flexible stamp, vertical component of stress $\sigma_y = const$ uniformly acts on the top surface of the oedometer.

The soil sample of the shear box with a stiff stamp, 0.071 in diameter and 0.035 in height, was discretised into 4-node tetrahedral elements (Fig 3). Three translatational degrees of freedom per node were considered for structural analysis. Displacement $u_y = const$ uniformly vertically acted on the top surface of the model.

![Fig 2](image2.png)  
**Fig 2.** Finite elements representation of the oedometer sample

![Fig 3](image3.png)  
**Fig 3.** Finite elements representation of the sample during the shear box test

While analysing the oedometer sample by numerical method, it was found that shear stress distribution in the sample was not uniform, and thus the vertical component of stress distributed also non-uniformly (Fig 4). A part of vertical load descends to shear ring pane. When the oedometer was analysed with the fixed ring and stiff stamp, it was obvious that whole sample is affected by the stress of compression and the upper corner by the stress of tension (Fig 5).
The stress and strain distribution in soil sample during the shear box test is non-uniform [22–25]. Applying a numerical method, horizontal soil displacements \( u_x \) in soil sample during shear box tests were analysed using stiff and flexible stamps. In Fig 6 we can see that the horizontal soil displacements \( u_x \) in shear box distribute non-uniformly. Fig 7 shows that vertical soil displacements reflect stamp turn: one side of stamp rises, the other – falls. Experiments demonstrate the same results.
The loading path is given in Fig 11. The Mohr envelope for a series of CU tests on sand specimens is shown in Fig 12. \( c' \) and \( \phi' \) according to experimental findings were calculated.

4.2. Experimental tests

In geotechnical laboratory a device was designed to analyse the non-uniform deformation of soil specimen caused by such factors as compaction of soil specimen, soil grading, shape and orientation of soil particles, magnitude of load etc.

The device consists of a metal cylinder of 15 cm in diameter and 45 cm height – 1, inside which there is a rubber membrane – 2. Metal cylinder was filled with a soil – 3. Inside the soil a steel strip – 4, 20 mm width and 0.5 mm thick was inserted. Steel strip was placed in 3 positions: in the centre of soil A and in the sides of soil B and C (Fig 13). After cylinder was filled with a soil, ends of cylinder were closed with plates – 5. Plates were screwed in order to stop leakage of air pressure. A sample of soil was subjected to an air pressure in the horizontal direction. Then the steel strip was loaded step by step by a vertical load till finally pulled out.

The same fine sand like triaxial sample and fine granite crushed stone of 0.5 mm were used for experiments. Soil samples were compacted and subjected to 25 kPa, 50 kPa, 75 kPa of confining air pressure. The density of sand 1.7 t/m\(^3\), void ratio 0.6. The density of fine granite crushed stone 1.4 t/m\(^3\), void ratio 0.95. Six experiments were carried out in one hole applying different confining air pressure. The experiment findings are presented in Figs 14–18. Experimental findings show that horizontal component of stress \( \sigma_x \) inside soil sample is distributed non-uniformly. Larger horizontal component of stress was found in the sides of soil specimen (side holes B,C) and smaller was found in the centre of soil specimen (middle hole–A). Figs 14, 16, 17, 18 show stresses, when steel strip from sand specimen was pulled out about 1–3 centimeters (continuous line) at first, and finally (dotted line) was pulled out at a larger force. It is not evident why.
Three types of samples with the density of 1.65 t/m$^3$ were prepared in order to estimate the influence of vertical component of stress on stress distribution in the soil samples. First sample, cylinder was full of sand (Figs 14, 16); the second sample, it is slightly more of sand in the cylinder than its length (Fig 17); the third sample contains slightly less sand in the cylinder than its length (Fig 18). Experimental results did not show an obvious influence. Displacements were not measured.

The pull-out force from fine granite crushed stone was larger, because its particles had a sharp shape. Thus, friction between a steel strip and particles of fine granite crushed stone was higher than between the steel strip and sand.

5. Conclusions

1. Mechanical properties of soils depend on construction of apparatus. Using different types of apparatus different stress-strain distribution was obtained.

2. The analysis of vertical component of stress $\sigma_y$ using the numerical method demonstrates a non-uniform distribution in soil specimens during oedometer, shear box and triaxial tests.

3. From the results of tests carried out in the laboratory it is obvious that horizontal component of stress $\sigma_x$ inside triaxial soil sample is distributed non-uniformly. Larger horizontal component of stress was found at the sides of soil specimen and smaller in the centre of soil specimen.

4. Analysis of references show that stress distribution in the triaxial soil samples are influenced by the friction between platens and sample ends.

5. Further experiments should be carried out in order to analyse stress distribution in the sample depending on soil density, soil grading, shape and orientation of soil particles, magnitude of load, ways of sample preparation, sample height and diameter ratio, friction between platens and sample ends etc.

References

Tvirtinant gruntų mechanines savybes laboratorijoje kiekviename aparate bandinys apkraunamas skirtingai. Tai turi įtakos įtempių ir deformacijų pasiskirstymui bandinėje. Interpretuojant bandymo duomenis ignoruojami tai kurie veiksmai, turintys įtaką įtempiams pasiskirstyti, pvz., bandinio galinių plokštumų ir štampo trinties įtakos tariant įtemptą odometre ar tiesioginio kirpimo aparate. Įtempių pasiskirstymo skaitinių modeliavimui nustatyta, kad ne tik odo mete ar tiesioginio kirpimo aparate, bet ir trišio slėgio aparate bandinio įtempiu būtų įvairių bandinio irėjimo trinties įtakos įtempamą ir tariant įtemptą odometre ar tiesioginio kirpimo aparate. Įtempių įtakos įtempiams pasiskirstymo skaitinius nustatyti

bandinėje, o tik tam tikraose jo taškuose. Žinant tikrąjį įtempimų ir deformacijų pasiskirstymą bandinėje, bus galima tiksliau nustatyti grunto mechaninių savybių rodiklius arba įvertinti tam tikrų veiksnių įtaką grunto savybių rodikliams.

Reikšminiai žodžiai: įtempimų ir deformacijų pasiskirstymas, triašio slėgio aparatas, odometras, tiesioginio kirpimo aparatas, skaičiums modeliavimas, grunto mechaninių savybių rodikliai.

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